

Traditional and present-day topics in real analysis

Dedicated to
Professor Jan Stanisław Lipiński



FACULTY OF MATHEMATICS
AND COMPUTER SCIENCE
UNIVERSITY OF ŁÓDŹ

„FOLIA MATHEMATICA”
SERIES EDITORS

Marek Śmietański, Piotr Fulmański, Cezary Obczyński

PROJECT EDITORS

Cezary Obczyński, Małgorzata Terepeta

COVER DESIGN

Mariusz Kubiński

PHOTOS

Małgorzata Terepeta

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**Dedicated to
Professor Jan Stanisław Lipiński
on the occasion of his 90th birthday**

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